

1. Express 250° in radians

$$250^\circ \left(\frac{\pi \text{ rads}}{180^\circ} \right) = \frac{250\pi}{180} = \boxed{\frac{25\pi}{18}}$$

2. Express $\frac{7\pi}{3}$ in degrees

$$\left(\frac{7\pi}{3} \right) \left(\frac{180^\circ}{\pi \text{ rads}} \right) = \frac{7(180)}{3\pi} = 7(60) = \boxed{420^\circ}$$

3. What is the coordinate of the point on the terminal side of $5\pi/6$

$$\left(-\frac{\sqrt{3}}{2}, \frac{1}{2} \right)$$

4. Evaluate the trigonometric function using its period as an aid: $\cos 5\pi$

$$\begin{aligned} \cos 5\pi &= \cos(5\pi - 2\pi) = \cos 3\pi = \cos(3\pi - 2\pi) \\ &= \cos \pi = \boxed{-1} \end{aligned}$$

5. Given $\cot \theta = 5/12$ and $\cos \theta > 0$, find $\sin \theta$

$$\begin{aligned} \cot \theta &= \frac{\text{adj}}{\text{opp}} \\ 5^2 + 12^2 &= c^2 \\ 13 &= c \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{\text{opp}}{\text{hyp}} \\ \sin \theta &= \boxed{\frac{12}{13}} \end{aligned}$$

6. Find the amplitude and period of $y = 3.25 \cos 3x$

$$\begin{aligned} \text{amp} &= |a| = \boxed{3.25} \\ \text{period} &= \frac{2\pi}{|b|} = \boxed{\frac{2\pi}{3}} \end{aligned}$$

7. Evaluate $\cos[\arcsin(1/2)]$

$$\begin{aligned} \arcsin\left(\frac{1}{2}\right) &\stackrel{\text{opp}}{\sim} \stackrel{\text{hyp}}{\sim} \\ 1^2 + a^2 &= 2^2 \\ a^2 &= 3 \\ a &= \sqrt{3} \end{aligned}$$

or think unit circle
 $\cos(\arcsin(1/2))$
 $\cos(\pi/6)$

$$\cos(\theta) = \frac{\sqrt{3}}{2}$$

8. Find a, b, c and d for $f(x) = d + a \cos(bx - c)$ so that the function matches the graph

Vertical shift up 3 units

$$d = 3$$

amplitude = 3

$$a = 3$$

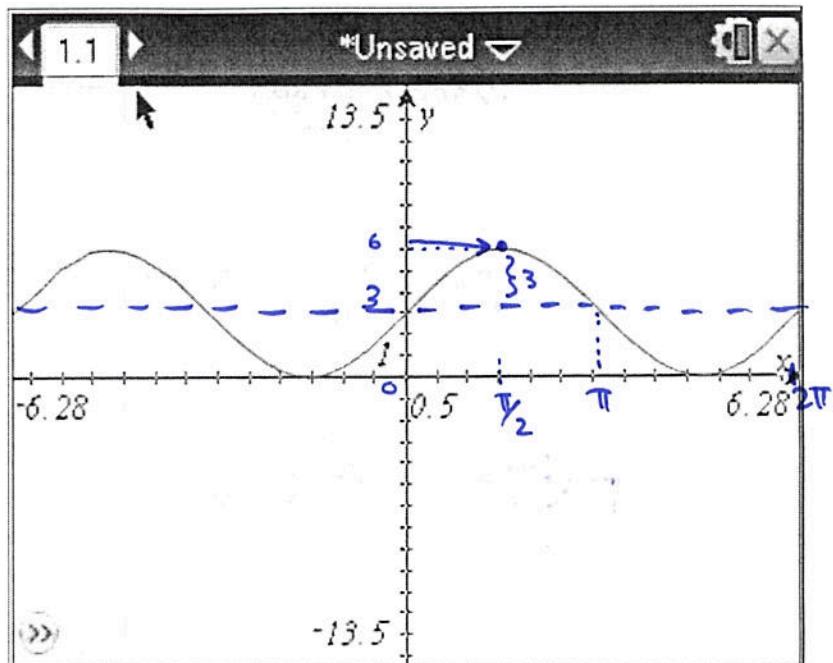
$$\text{period} = \frac{2\pi}{|b|} = 2\pi$$

$$2\pi = 2\pi b \\ 1 = b$$

horizontal shift right $\frac{\pi}{2}$
(phase)

$$f(x) = 3(\cos(1(x - \frac{\pi}{2}))) + 3$$

$$f(x) = 3 + 3\cos(x - \frac{\pi}{2})$$



$$2\pi = 6.28318$$

9. Find the amplitude and period of the function graphed at the right:

$$\text{Amp} = 3$$

$$\text{Period} = 4\pi$$

$$\text{amp} = 3 = a$$

$$\text{period} = \frac{2\pi}{b} = 4\pi$$

$$2\pi = 4\pi b$$

$$\frac{1}{2} = b$$

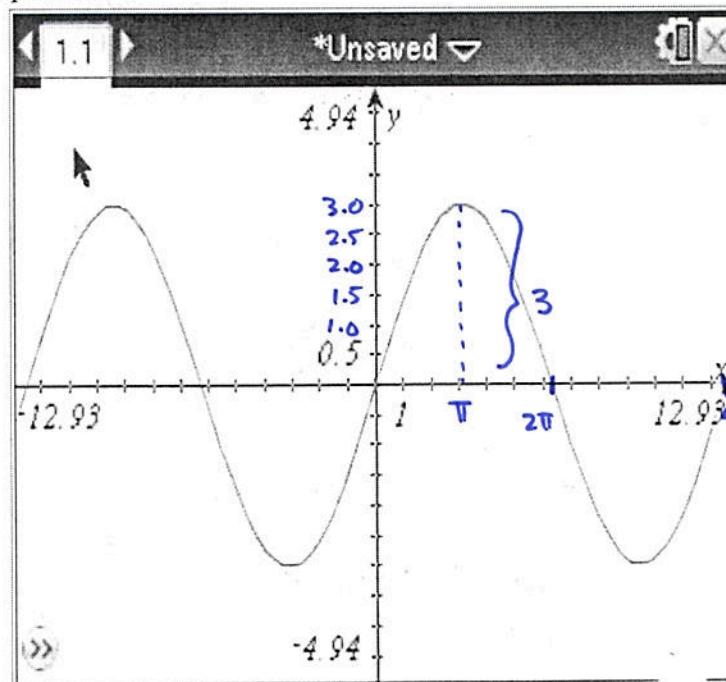
no vertical shift

phase shift for $\cos x \rightarrow \pi$ units right

10. Write the equation of the function whose graph is at the right.

$$f(x) = 3 \sin(\frac{1}{2}x)$$

$$\text{or } f(x) = 3 \cos(\frac{1}{2}(x - \pi)) \\ = 3 \cos(\frac{1}{2}x - \frac{\pi}{2})$$



$$2\pi = 6.28318$$

11. Determine the quadrant of the following: $\frac{13\pi}{3}$

$$\frac{13\pi}{3} - 2\pi$$

$$\frac{7\pi}{3} - 2\pi$$

$$\frac{13\pi}{3} - \frac{6\pi}{3} = \frac{7\pi}{3}$$

$$\frac{7\pi}{3} - \frac{6\pi}{3} = \frac{\pi}{3}$$

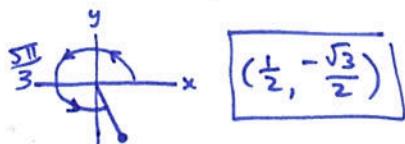
Quadrant I

12. Express the following in radians: 445°

$$445^\circ \left(\frac{\pi \text{ rad}}{180^\circ} \right) = \frac{445 \pi}{180} = \frac{89\pi}{36}$$

13. Find the point (a,b) on the unit circle that corresponds to the real number t : $t = \frac{5\pi}{3}$

Then find sine, cosine and tangent.

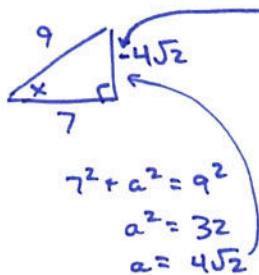


$$\sin(\frac{5\pi}{3}) = -\frac{\sqrt{3}}{2}$$

$$\cos(\frac{5\pi}{3}) = \frac{1}{2}$$

$$\tan(\frac{5\pi}{3}) = \frac{\sin(\frac{5\pi}{3})}{\cos(\frac{5\pi}{3})} = \frac{-\sqrt{3}/2}{1/2} = -\sqrt{3}$$

14. Find $\cot x$: If $\cos x = 7/9$, $\sin x < 0$



$$\cot x = \frac{\cos x}{\sin x}$$

or $\frac{\text{adj}}{\text{opp}}$... ☺

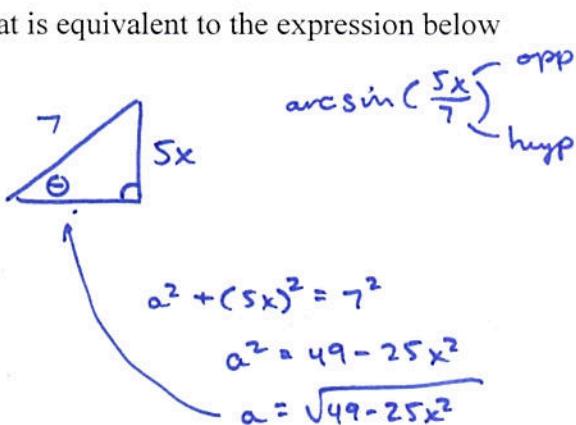
15. Find an algebraic expression that is equivalent to the expression below

$$\cot(\arcsin(5x/7))$$

... cot(θ)

$$\frac{\sqrt{49-25x^2}}{5x}$$

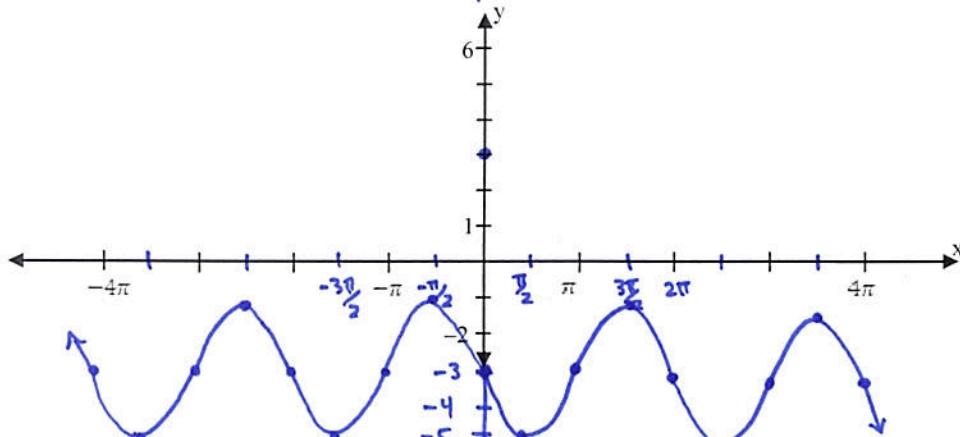
adj
opp



16. Sketch the graph. Show TWO (2) full periods

$$f(x) = -2\sin(x) - 3$$

vertical shift down 3 units
amplitude = 2
reflect over x-axis



17. Given the equation $y = 2\sin(3x - \pi) - 5$, find the following $\rightarrow y = 2\sin(3(x - \frac{\pi}{3})) - 5$

Amplitude: $a = 2$

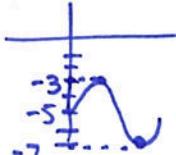
Period: $\frac{2\pi}{b} = \frac{2\pi}{3}$

Horizontal Shift: right $\frac{\pi}{3}$ units

Vertical Shift: down 5 units

Domain: $(-\infty, \infty)$

Range: $[-7, -3]$



18. Evaluate $\csc 17.2^\circ$

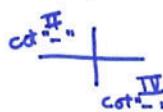
3.382

19. Find the amplitude and period $2 \sin \frac{x\pi}{3} = 2\sin(\frac{\pi}{3}x)$

Amp = 2

Period = $\frac{2\pi}{b} = \frac{2\pi}{\frac{\pi}{3}} = 2\pi \cdot \frac{3}{\pi} = 6$

20. Approximate TWO values of θ ($0^\circ \leq \theta < 360^\circ$) that satisfies the equation. Round to three decimal places.



$\cot \theta = -0.5$

$\theta = \cot^{-1}(-0.5)$

$\theta = 116.565^\circ$

$\theta = 180 + 116.565^\circ$

$= 296.565^\circ$

21. Evaluate with a calculator: $\sin(2\pi/3)$

$\frac{\sqrt{3}}{2} = .866$