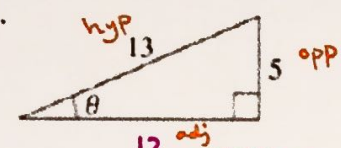
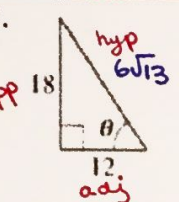


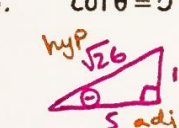
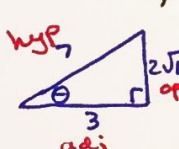
### STATION 1

Find the exact values of the six trigonometric functions of the angle  $\theta$  shown in the figure.

|  |   |   |
|--|---|---|
| <p>1.</p>  <p>hyp 13<br/>opp 5<br/>adj 12</p> <p>☺... (5, 12, 13)<br/> <math>a^2 + 5^2 = 13^2</math><br/> <math>a^2 + 25 = 169</math><br/> <math>a^2 = 144</math><br/> <math>a = 12</math></p>  | $\sin \theta = \frac{5}{13}$ $\cos \theta = \frac{12}{13}$ $\tan \theta = \frac{5}{12}$   | $\csc \theta = \frac{13}{5}$ $\sec \theta = \frac{13}{12}$ $\cot \theta = \frac{12}{5}$           |
| <p>2.</p>  <p>opp 18<br/>hyp <math>6\sqrt{3}</math><br/>adj 12</p> <p>☺...<br/> <math>12^2 + 18^2 = c^2</math><br/> <math>144 + 324 = c^2</math><br/> <math>468 = c^2</math><br/> <math>\sqrt{468} = c</math><br/> <math>6\sqrt{3} = c</math></p> | $\sin \theta = \frac{18}{6\sqrt{3}} = \frac{3}{\sqrt{3}}$ $\cos \theta = \frac{12}{6\sqrt{3}} = \frac{2}{\sqrt{3}}$ $\tan \theta = \frac{18}{12} = \frac{3}{2}$ | $\csc \theta = \frac{\sqrt{3}}{3}$ $\sec \theta = \frac{\sqrt{3}}{2}$ $\cot \theta = \frac{2}{3}$ |

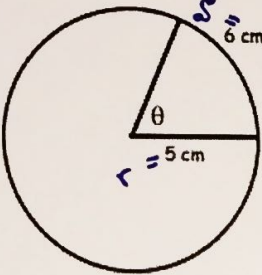
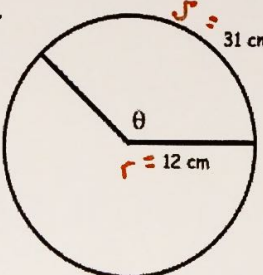
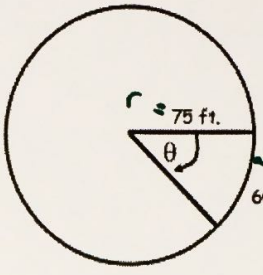
### STATION 2

Sketch a right triangle corresponding to the trigonometric function of the acute angle  $\theta$ . Then find the other five trigonometric functions of  $\theta$ .

|  |   |   |
|--|---|---|
| <p>3. <math>\cot \theta = 5 = \frac{5 \text{ adj}}{1 \text{ opp}}</math> ☺</p>  <p>hyp <math>\sqrt{26}</math><br/>opp 1<br/>adj 5</p> <p><math>5^2 + 1^2 = c^2</math><br/> <math>26 = c^2</math><br/> <math>\sqrt{26} = c</math></p>                                      | $\sin \theta = \frac{1}{\sqrt{26}}$ $\cos \theta = \frac{5}{\sqrt{26}}$ $\tan \theta = \frac{1}{5}$ | $\csc \theta = \sqrt{26}$ $\sec \theta = \frac{\sqrt{26}}{5}$   |
| <p>4. <math>\cos \theta = \frac{3}{7} = \frac{\text{adj}}{\text{hyp}}</math> ☺</p>  <p>hyp 7<br/>opp <math>2\sqrt{10}</math><br/>adj 3</p> <p><math>a^2 + 3^2 = 7^2</math><br/> <math>a^2 + 9 = 49</math><br/> <math>a^2 = 40</math><br/> <math>a = 2\sqrt{10}</math></p> | $\sin \theta = \frac{2\sqrt{10}}{7}$ $\tan \theta = \frac{2\sqrt{10}}{3}$                           | $\csc \theta = \frac{7}{2\sqrt{10}}$ $\sec \theta = \frac{7}{3}$ $\cot \theta = \frac{3}{2\sqrt{10}}$ |

### STATION 3

Find the angle in radians.

|   |  |
|---|--|
| <p>1.</p>  <p> <math>s = r\theta</math><br/> <math>6 = 5\theta</math><br/> <math>6/5 = \theta</math><br/> <math>\theta = 1.2 \text{ radians}</math> </p>             | <p>2.</p>  <p> <math>s = r\theta</math><br/> <math>31 = 12\theta</math><br/> <math>\frac{31}{12} = \theta</math><br/> <math>\theta = 2.583 \text{ radians}</math> </p> |
| <p>3. <math>r =</math> radius is 7 meters<br/> <math>s =</math> arc length is 32 meters</p> <p> <math>s = r\theta</math><br/> <math>32 = 7\theta</math><br/> <math>\frac{32}{7} = \theta</math><br/> <math>\theta = 4.571 \text{ radians}</math> </p> | <p>4.</p>  <p> <math>s = r\theta</math><br/> <math>60 = 75\theta</math><br/> <math>\frac{60}{75} = \theta</math><br/> <math>\theta = 0.8 \text{ rads}</math> </p>      |

### STATION 4

Find the length of the arc.

|   |   |
|---|---|
| <p>5. <math>r =</math> radius is 14 inches<br/> <math>\theta =</math> central angle <math>\theta</math> is <math>180^\circ</math></p> <p> <math>\theta = (180^\circ) \left( \frac{\pi}{180^\circ} \right) = \pi \text{ radians}</math><br/> <math>s = r\theta</math><br/> <math>s = 14(\pi)</math><br/> <math>s = 14\pi \text{ inches}</math><br/>         or <math>43.982 \text{ inches}</math> </p> | <p>6. <math>r =</math> radius is 12 centimeters<br/> <math>\theta =</math> central angle <math>\theta</math> is <math>\frac{3\pi}{4}</math></p> <p> <math>s = r\theta</math><br/> <math>s = 12 \left( \frac{3\pi}{4} \right)</math><br/> <math>s = 9\pi \text{ cm}</math><br/>         or <math>28.274 \text{ cm}</math> </p> |
|---|---|

Find the radius.

|  |  |
|--|--|
| <p>7. <math>s =</math> arc length is 36 feet<br/> <math>\theta =</math> central angle <math>\theta</math> is <math>\frac{\pi}{2}</math></p> <p> <math>s = r\theta</math><br/> <math>\frac{2}{\pi} \cdot 36 = r \left( \frac{\pi}{2} \right) \cdot \frac{2}{\pi}</math><br/> <math>\frac{72}{\pi} = r</math><br/> <math>r = 22.918 \text{ ft}</math> </p> | <p>8. <math>s =</math> arc length is 82 miles<br/> <math>\theta =</math> central angle <math>\theta</math> is <math>135^\circ</math></p> <p> <math>\theta = 135^\circ \left( \frac{\pi}{180^\circ} \right) = \frac{3\pi}{4} \text{ radians}</math><br/> <math>s = r\theta</math><br/> <math>\frac{4}{3\pi} \cdot 82 = r \left( \frac{3\pi}{4} \right) \cdot \frac{4}{3\pi}</math><br/> <math>\frac{328}{3\pi} = r</math><br/> <math>r = 34.802 \text{ miles}</math> </p> |
|--|--|



### STATION 5

Use the blank unit circle to mark the angle and then label the point. Then evaluate (if possible) the sine, cosine, and tangent of the real number  $t$ .

|   |  |  |
|---|--|--|
| <p>7. <math>t = \frac{7\pi}{6}</math></p> <p><math>\sin t = -\frac{1}{2}</math>     <math>\sin \theta = y</math><br/> <math>\cos t = -\frac{\sqrt{3}}{2}</math>     <math>\cos \theta = x</math><br/> <math>\tan t = \frac{-1/2}{-\sqrt{3}/2} = \frac{1}{\sqrt{3}}</math>     <math>\tan \theta = \frac{y}{x}</math><br/> <math>\tan t = \frac{1}{\sqrt{3}}</math> or <math>\frac{\sqrt{3}}{3}</math></p> | <p>8. <math>t = \frac{2\pi}{3}</math></p> <p><math>\sin t = \frac{\sqrt{3}}{2}</math><br/> <math>\cos t = -\frac{1}{2}</math><br/> <math>\tan t = \frac{\sqrt{3}/2}{-1/2} = -\sqrt{3}</math></p> | <p>9. <math>t = -\frac{5\pi}{3}</math></p> <p><math>\sin t = \frac{\sqrt{3}}{2}</math><br/> <math>\cos t = \frac{1}{2}</math><br/> <math>\tan t = \frac{\sqrt{3}/2}{1/2} = \sqrt{3}</math></p> |
|---|--|--|

### STATION 6

Draw each angle in standard position (initial & terminal sides). Determine the reference angle (if it's not quadrantal). Find one positive and one negative angle that is coterminal to each angle (answers may vary).

|   |  |  |   |
|---|--|--|---|
| <p>1. <math>-50^\circ</math></p> <p>Ref. <math>\angle = 50^\circ</math><br/> Coterminal <math>\angle</math>s:<br/> <math>310^\circ, -410^\circ</math></p> | <p>2. <math>\frac{4\pi}{3}</math></p> <p>Ref. <math>\angle = \frac{\pi}{3}</math><br/> Coterminal <math>\angle</math>s:<br/> <math>-\frac{2\pi}{3}, \frac{10\pi}{3}</math></p> | <p>3. <math>420^\circ</math></p> <p>Ref. <math>\angle = 60^\circ</math><br/> Coterminal <math>\angle</math>s:<br/> <math>60^\circ, -300^\circ</math></p> | <p>4. <math>-\frac{5\pi}{6}</math></p> <p>Ref. <math>\angle = \frac{\pi}{6}</math><br/> Coterminal <math>\angle</math>s:<br/> <math>\frac{7\pi}{6}, -\frac{17\pi}{6}</math></p> |
|---|--|--|---|

$360^\circ - 50^\circ = 310^\circ$   
 $-50^\circ - 360^\circ = -410^\circ$   
 $\frac{4\pi}{3} - 2\pi = \frac{4\pi}{3} - \frac{6\pi}{3} = -\frac{2\pi}{3}$   
 $\frac{4\pi}{3} + 2\pi = \frac{4\pi}{3} + \frac{6\pi}{3} = \frac{10\pi}{3}$   
 $420^\circ - 360^\circ = 60^\circ$   
 $420^\circ - 360^\circ - 360^\circ = -300^\circ$   
 $-\frac{5\pi}{6} + 2\pi = -\frac{5\pi}{6} + \frac{12\pi}{6} = \frac{7\pi}{6}$   
 $-\frac{5\pi}{6} - 2\pi = -\frac{5\pi}{6} - \frac{12\pi}{6} = -\frac{17\pi}{6}$

## STATION 7

### CALCULATOR

Rewrite each angle in radian measure in the following ways:

- a) in terms of  $\pi$   
 b) the rounded decimal equivalent (round three decimal places)

|  |  |  |  |
|--|--|--|--|
| 34. $145^\circ$<br>a) $145^\circ \left(\frac{\pi}{180^\circ}\right) = \frac{29}{36} \pi$<br>b) <span style="border: 1px solid black; padding: 2px;">2.531</span> | 35. $-80^\circ$<br>a) $-80^\circ \left(\frac{\pi}{180^\circ}\right) = -\frac{4}{9} \pi$<br>b) <span style="border: 1px solid black; padding: 2px;">-1.396</span> | 36. $-350^\circ$<br>a) $-350^\circ \left(\frac{\pi}{180^\circ}\right) = -\frac{35}{18} \pi$<br>b) <span style="border: 1px solid black; padding: 2px;">-6.109</span> | 37. $58^\circ$<br>a) $58^\circ \left(\frac{\pi}{180^\circ}\right) = \frac{29}{90} \pi$<br>b) <span style="border: 1px solid black; padding: 2px;">1.012</span> |
|--|--|--|--|

Rewrite each angle in degree measure. Round three decimal places when needed.

|  |  |   |   |
|--|--|---|---|
| 38. $\frac{6\pi}{5}$<br>$\left(\frac{6\pi}{5}\right) \left(\frac{180^\circ}{\pi}\right) = \span style="border: 1px solid black; padding: 2px;">216^\circ $ | 39. $-\frac{4\pi}{3}$<br>$-\frac{4\pi}{3} \left(\frac{180^\circ}{\pi}\right) = \span style="border: 1px solid black; padding: 2px;">-240^\circ $ | 40. $5\pi$<br>$5\pi \left(\frac{180^\circ}{\pi}\right) = \span style="border: 1px solid black; padding: 2px;">900^\circ $ | 41. $5$<br>$5 \left(\frac{180^\circ}{\pi}\right) = \span style="border: 1px solid black; padding: 2px;">286.479^\circ $ |
|--|--|---|---|

## STATION 8

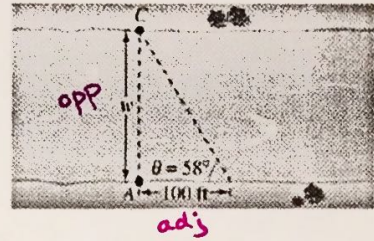
Answer the following. Provide an exact value (in terms of  $\pi$ ) and decimal value (rounded to three places).

|  |  |   |
|--|--|---|
| 50. An arc of a circle has a central angle measure of $330^\circ$ and a length of 15 feet. Find the length of a <u>radius</u> of the circle.<br>$\theta = 330^\circ \rightarrow 330^\circ \left(\frac{\pi}{180^\circ}\right) = \frac{11\pi}{6}$<br>$s = 15 \text{ ft} \quad r = ?$<br>$s = r\theta$<br>$\frac{6}{11\pi} \cdot 15 = r \left(\frac{11\pi}{6}\right) \cdot \frac{6}{11\pi}$<br>$\frac{90}{11\pi} \text{ ft} = r$<br><span style="border: 1px solid black; padding: 2px;"><math>r = 0.074 \text{ ft}</math></span> | 51. Find the length of an arc of a circle with a radius of 25 cm and a central angle measure of $\frac{3\pi}{7}$ .<br>$r = 25 \text{ cm} \quad \theta = \frac{3\pi}{7} \quad s = ?$<br>$s = r\theta$<br>$s = 25 \left(\frac{3\pi}{7}\right)$<br><span style="border: 1px solid black; padding: 2px;"><math>s = \frac{75}{7} \pi \text{ cm}</math></span><br><span style="border: 1px solid black; padding: 2px;"><math>s = 33.660 \text{ cm}</math></span> | 52. Find the measure of a central angle of an arc if its length is 10 meters and the radius is 2 meters.<br>$s = 10 \text{ m} \quad r = 2 \text{ m} \quad \theta = ?$<br>$s = r\theta$<br>$10 = 2\theta$<br>$5 = \theta$<br><span style="border: 1px solid black; padding: 2px;"><math>\theta = 5 \text{ radians}</math></span> |
|--|--|---|



### STATION 9

21. A biologist wants to know the width  $w$  of a river (see figure) in order to properly set instruments for studying the pollutants in the water. From point  $A$ , the biologist walks downstream 100 feet and sights to point  $C$ . From the sighting, it is determined that  $\theta = 58^\circ$ . How wide is the river? Round your answer to three decimal places.



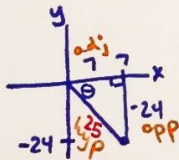
$$\tan 58^\circ = \frac{w}{100}$$

$$w = 100 \tan 58^\circ$$

$$w = 160.033 \text{ ft}$$

### STATION 10

24. Find the 6 trigonometric function values for the point  $(7, -24)$  on the terminal side of angle  $\theta$ .



$$\sin \theta = \frac{-24}{25} \quad \csc \theta = \frac{-25}{24}$$

$$\cos \theta = \frac{7}{25} \quad \sec \theta = \frac{25}{7}$$

$$\tan \theta = \frac{-24}{7} \quad \cot \theta = \frac{-7}{24}$$

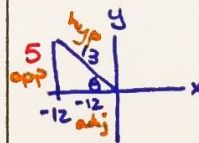
☺ ∴ (7, 24, 25)

$$\begin{aligned} 7^2 + (-24)^2 &= c^2 \\ 49 + 576 &= c^2 \\ 625 &= c^2 \\ 25 &= c \end{aligned}$$

25. Given that  $\cos \theta = -\frac{12}{13}$  and  $\sin \theta > 0$ , find the exact values of the other five trig. functions.

Quadrant II,  $\cos \theta < 0$   
 $\sin \theta > 0$

☺  
 $x < 0$   
 $y > 0$



$$\sin \theta = \frac{5}{13} \quad \csc \theta = \frac{13}{5}$$

$$\cos \theta = -\frac{12}{13} \quad \sec \theta = -\frac{13}{12}$$

$$\tan \theta = \frac{5}{-12} \quad \cot \theta = -\frac{12}{5}$$

☺ ∴ (5, 12, 13)

$$\begin{aligned} a^2 + (-12)^2 &= 13^2 \\ a^2 + 144 &= 169 \\ a^2 &= 25 \\ a &= 5 \end{aligned}$$