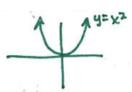
## 1.2 Functions and Their Properties Domain, Range, & Continuity of Functions

Target 1B: Analyze functions using specific properties

Review of Prior Concepts

Is the formula a function? (Graph them to complete the vertical line test).

1.  $v = x^2$ 



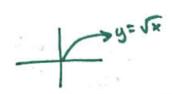
2.  $v^2 = x$ 



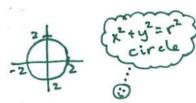
posses vertical line test .. , y= x is afunction

fails vartical line test :, y2=x is NOT a function

**3.** 
$$y = \sqrt{x}$$



**4.**  $x^2 + y^2 = 4$ 



passes vertical line test :, y= Jx is a function

fails vertical line test

.: , x2+y2=4 is NOT a function

#### **More Practice**

#### Is it a Function?

http://www.mathwarehouse.com/algebra/relation/vertical-line-test.php

https://www.youtube.com/watch?v=zT69oxcMhPw

https://www.khanacademy.org/math/cc-eighth-grade-math/cc-8th-linear-equations-functions/cc-8th-

function-intro/e/recog-func-2

#### **SAT Connection**

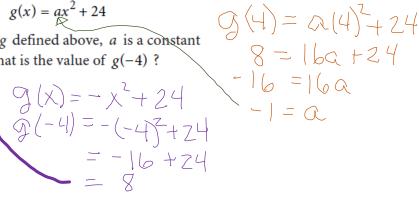
## **Passport to Advanced Math**

**13.** Use function notation, and interpret statements using function notation.

Example:

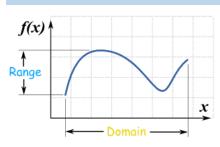
$$g(x) = ax^2 + 24$$

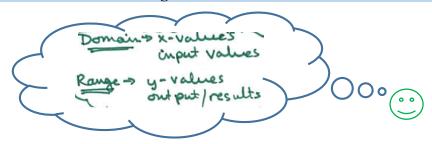
For the function g defined above, a is a constant and g(4) = 8. What is the value of g(-4)?



# Solution

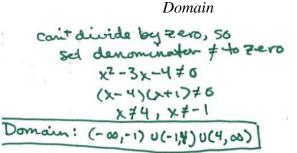
### **Domain & Range**

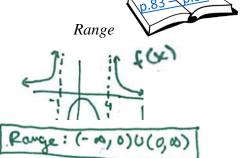




Find the domain algebraically & the range graphically of each function. Example 1:

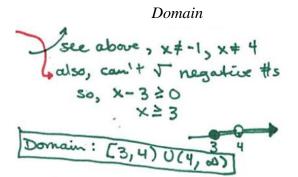
 $f(x) = \frac{2}{x^2 - 3x - 4}$ 

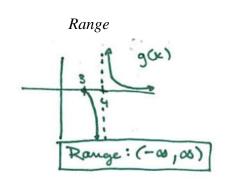




Example 2:

$$g(x) = \frac{\sqrt{x-3}}{x^2 - 3x - 4}$$





Example 3:

$$h(x) = \frac{x^2}{x^2 - 3x}$$

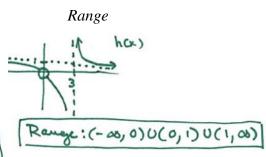
Domain
$$x^{2}-3x+0$$

$$x(x-3)+0$$

$$x\neq 0, x-3\neq 0$$

$$y\neq 3$$

Domain: (-00,0) U(0,3) U(3,00)



**More Practice** 

## Domain & Range

http://www.coolmath.com/algebra/15-functions/06-finding-the-domain-01 https://www.khanacademy.org/math/algebra/algebra-functions/domain-and-range/v/domain-of-a-function-intro http://www.intmath.com/functions-and-graphs/2a-domain-and-range.php

## **Continuity & Discontinuity**

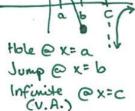
• Functions are continuous if there are not jumps, holes or asymptotes (no breaks in the graphs)



• Removable discontinuity

(can make the discontinuity go away) HOLE in the graph @ x=a

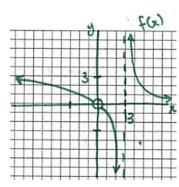
· Non-removable discontinuity (cont make discort, go away)



- O JUMP
- o INFINITE (vertical asymptote)

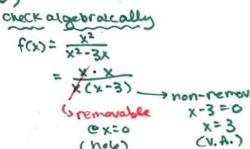
Graph the function. Identify any points of discontinuity and describe the type of discontinuity.

Example 4: 
$$f(x) = \frac{x^2}{x^2 - 3x}$$

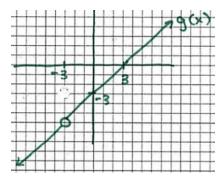


infinite discontinuity (non-removable)
@ x=3

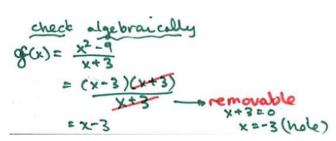
hole @ x=0 (removable)



Example 5:  $g(x) = \frac{x^2 - 9}{x + 3}$ 



hole @ x=-3 (removable)



#### **More Practice**

## Continuity

http://www.ck12.org/Analysis/Discrete-and-Continuous-Functions/lesson/Continuity-and-Discontinuity-PCALC/

https://www.youtube.com/watch?v=2n5VzMFJQVY

## **SAT Connection**

#### Solution

**Choice A is correct.** Since *g* is an even function, g(-4) = g(4) = 8.

Alternatively: First find the value of a, and then find g(-4). Since g(4) = 8, substituting 4 for x and 8 for g(x) gives  $8 = a(4)^2 + 24 = 16a + 24$ . Solving this last equation gives a = -1. Thus  $g(x) = -x^2 + 24$ , from which it follows that  $g(-4) = -(-4)^2 + 24$ ; g(-4) = -16 + 24; and g(-4) = 8.

Choices B, C, and D are incorrect because g is a function and there can only be one value of g(-4).