

**Limits at Infinity****2003 AP Multiple-Choice Non-Calculator**

6.  $\lim_{x \rightarrow \infty} \frac{x^3 - 2x^2 + 3x - 4}{4x^3 - 3x^2 + 2x - 1} =$

- (A) 4      (B) 1      (C)  $\frac{1}{4}$       (D) 0      (E) -1

**2008 AP Multiple-Choice Non-Calculator**

1.  $\lim_{x \rightarrow \infty} \frac{(2x-1)(3-x)}{(x-1)(x+3)}$  is

- (A) -3      (B) -2      (C) 2      (D) 3      (E) nonexistent

**Limits at Infinity** – end behavior of a graph/function

– Horizontal Asymptote at  $y = L$  if  $\lim_{x \rightarrow \infty} f(x) = L$  or  $\lim_{x \rightarrow -\infty} f(x) = L$ .

If degree of numerator  $\leq$  degree of denominator, then  $\lim_{x \rightarrow \pm\infty} f(x) =$

(and, Horizontal Asymptote at  $y =$  )

*Example:* Evaluate the limit, if the limit exists.

$$\lim_{x \rightarrow \infty} \frac{5x^2 - 3x + 1}{7x^2 - 4}$$

If degree of numerator  $\geq$  degree of denominator, then  $\lim_{x \rightarrow \pm\infty} f(x) =$

(and, Horizontal Asymptote at  $y =$  )

*Example:* Evaluate the limit, if the limit exists.

$$\lim_{x \rightarrow \infty} \frac{7x+1}{5x^2 - 4}$$

If degree of numerator  $<$  degree of denominator, then  $\lim_{x \rightarrow \pm\infty} f(x) =$

(and, NO Horizontal Asymptote)

*Example:* Evaluate the limit, if the limit exists.

$$\lim_{x \rightarrow \infty} \frac{5x^2 - 3x + 1}{7x - 4}$$