

Arc Length (Parametric & Vectors)

1. The length of the path described by the parametric equations $x = \cos^3 t$ and $y = \sin^3 t$, for $0 \leq t \leq \frac{\pi}{2}$, is given by

(A) $\int_0^{\pi/2} \sqrt{3 \cos^2 t + 3 \sin^2 t} dt$

(B) $\int_0^{\pi/2} \sqrt{-3 \cos^2 t \sin t + 3 \sin^2 t \cos t} dt$

(C) $\int_0^{\pi/2} \sqrt{9 \cos^4 t + 3 \sin^4 t} dt$

(D) $\int_0^{\pi/2} \sqrt{9 \cos^4 t \sin^2 t + 3 \sin^4 t \cos^2 t} dt$

(E) $\int_0^{\pi/2} \sqrt{\cos^6 t + \sin^6 t} dt$

2. A particle move in the xy -plane so that its position at any time t is given by $x(t) = t^2$ and $y(t) = \sin(4t)$. What is the speed of the particle when $t = 3$?

- (A) 2.909
- (B) 3.062
- (C) 6.884
- (D) 9.016
- (E) 47.393

3. For $t \geq 0$, a particle is moving along a curve that that its position at time t is $(x(t), y(t))$.

At time $t = 2$, the particle is at position $(1, 5)$. It is known that $\frac{dx}{dt} = \frac{\sqrt{t+2}}{e^t}$ and $\frac{dy}{dt} = \sin^2 t$. Find the speed of the particle at time $t = 4$. Find the distance traveled by the particle from time $t = 2$ to $t = 4$.