

$$p > 2$$

The series

$$\sum_{n=1}^{\infty} \frac{n^2 + 1}{n^4 + 1}$$

- (A) converges by the Ratio Test.
- (B) diverges by the Integral Test.
- (C) converges by the Limit Comparison Test with the series $\sum_{n=1}^{\infty} \frac{1}{n^2}$
- (D) diverges by the Limit Comparison Test with the series $\sum_{n=1}^{\infty} \frac{1}{n}$

C

Consider the series:

$$\sum_{n=1}^{\infty} \frac{e^n}{n!}$$

If the ratio test is applied to the series, which of the following inequalities results, implying that the series converges?

(A) $\lim_{n \rightarrow \infty} \frac{e}{n!} < 1$

(B) $\lim_{n \rightarrow \infty} \frac{n!}{e} < 1$

(C) $\lim_{n \rightarrow \infty} \frac{n+1}{e} < 1$

(D) $\lim_{n \rightarrow \infty} \frac{e}{n+1} < 1$

(E) $\lim_{n \rightarrow \infty} \frac{e}{(n+1)!} < 1$

D

Which statement is true about the series:

$$\sum_{n=1}^{\infty} e^{2/n}$$

- (A) The nth term test concluded that the series converges.
- (B) The nth term test concluded that the series diverges.
- (C) The nth term test hypotheses are not met by this series, so the nth term test cannot be applied.
- (D) The nth term test hypotheses are met by this series; however, the nth term test is inconclusive.
- (E) None of the above are true.

B

Determine whether the following series converges or diverges:

$$\sum_{n=1}^{\infty} \frac{\sqrt{n} + 1}{e^n}$$

The series converges by
the ratio test.

Determine whether the following series converges or diverges:

$$\sum_{n=1}^{\infty} \frac{\sqrt{n^2 + n^3}}{3n^2 + 7n}$$

The series diverges by the limit comparison test.

Determine whether the following series converges or diverges by
using the integral test.

$$\sum_{n=1}^{\infty} \frac{2n}{n^2 + 1}$$

The series diverges by the integral test.

What are all values of p for which the series

$$\sum_{n=1}^{\infty} \frac{n}{n^p + 1}$$

converges?