

2.3 Removable + Non Removable Discontinuities

Removable - can eliminate the discontinuity algebraically

- HOLE (graphically)
- no values in table (numerically)

Non Removable - can't eliminate the discontinuity algebraically

- V.A., JUMPS (graphically)

- no values in table and

$$\lim_{x \rightarrow c^-} f(x) \neq \lim_{x \rightarrow c^+} f(x)$$

(numerically)

Find discontinuities in the function and identify the type.

ex: $f(x) = \frac{x^2 - 1}{x^2 - x - 2}$

$$= \frac{(x+1)(x-1)}{(x+1)(x-2)}$$

nonremovable
discont (V.A.)
@ $x=2$

removable discont (hole)
 $x = -1$

ex: Find discontinuities and sketch the graph

$$f(x) = \frac{x}{x^2 - 3x}$$

$$= \frac{x}{x(x-3)}$$

nonremovable (VA) discontinuity @ $x=3$

removable discontinuity @ $x=0$

$$f(x) = \frac{1}{x-3}$$

$$f(0) = \frac{1}{0-3} = -\frac{1}{3}$$

