

Name _____

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Rally Coach: Take turns solving problems.

Simplify.

1) $(-2+7i)^2$

$$\begin{aligned} & (-2+7i)(-2+7i) \\ & 4 - 14i - 14i + 49i^2 \\ & 4 - 28i + 49(-1) \\ & 4 - 28i - 49 \\ & \boxed{-45 - 28i} \end{aligned}$$

3) $\frac{-3+6i}{6+3i} \cdot \frac{6-3i}{6-3i}$

$$\begin{aligned} & = \frac{(-3+6i)(6-3i)}{(6+3i)(6-3i)} \\ & = \frac{-18 + 36i + 9i - 18i^2}{36 - 18i + 18i - 9i^2} \\ & = \frac{-18 + 45i - 18(-1)}{36 - 9(-1)} \\ & = \frac{-18 + 45i + 18}{36 + 9} = \frac{45i}{45} \\ & = \boxed{i} \end{aligned}$$

2) $(3-6i)^2$

$$\begin{aligned} & (3-6i)(3-6i) \\ & 9 - 18i - 18i + 36i^2 \\ & 9 - 36i + 36(-1) \\ & 9 - 36i - 36 \\ & \boxed{-27 - 36i} \end{aligned}$$

4) $\frac{-4-i}{2+2i} \cdot \frac{2-2i}{2-2i}$

$$\begin{aligned} & = \frac{(-4-i)(2-2i)}{(2+2i)(2-2i)} \\ & = \frac{-8 - 2i + 8i + 2i^2}{4 - 4i + 4i - 4i^2} \\ & = \frac{-8 + 6i + 2(-1)}{4 - 4(-1)} \\ & = \frac{-8 + 6i + 2}{4 + 4} = \frac{-10 + 6i}{8} \\ & = \frac{-10}{8} + \frac{6}{8}i \\ & = \boxed{-\frac{5}{4} + \frac{3}{4}i} \end{aligned}$$

Solve each equation with the quadratic formula.

5) $x^2 + 9 = 2x$

$x^2 - 2x + 9 = 0$

$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(9)}}{2(1)}$

$= \frac{2 \pm \sqrt{4 - 36}}{2}$

$= \frac{2 \pm \sqrt{-32}}{2}$

$= \frac{2 \pm \sqrt{16 \cdot -2}}{2}$

$= \frac{2 \pm 4i\sqrt{2}}{2}$

$= \frac{2}{2} \pm \frac{4i\sqrt{2}}{2} \rightarrow 1 + 2i\sqrt{2}$

$$\begin{aligned} & x = 1 + 2\sqrt{2}i, \\ & x = 1 - 2\sqrt{2}i \end{aligned}$$

6) $11n^2 = -2 - 4n$

$11n^2 + 4n + 2 = 0$

$x = \frac{-4 \pm \sqrt{4^2 - 4(11)(2)}}{2(11)}$

$= \frac{-4 \pm \sqrt{16 - 88}}{22}$

$= \frac{-4 \pm \sqrt{-72}}{22}$

$= \frac{-4 \pm \sqrt{36 \cdot -2}}{22}$

$= \frac{-4 \pm 6i\sqrt{2}}{22}$

$= \frac{-4}{22} \pm \frac{6i\sqrt{2}}{22}$

$= \frac{-2}{11} \pm \frac{3i\sqrt{2}}{11}$

$$\begin{aligned} & x = \frac{-2}{11} + \frac{3i\sqrt{2}}{11}, \\ & x = \frac{-2}{11} - \frac{3i\sqrt{2}}{11} \end{aligned}$$

Write a polynomial function of least degree with integral coefficients that has the given zeros.

7) $-2i, 2i, 1-i, 1+i$

$$x = -2i, x = 2i, x = 1-i, x = 1+i$$

$$x+2i=0 \quad x-2i=0 \quad x-1+i=0 \quad x-1-i=0$$

$$f(x) = (x+2i)(x-2i)(x-1+i)(x-1-i)$$

$$= (x^2 + 2ix - 2ix - 4i^2)(x^2 - x - ix - x + 1 + i - i - i^2)$$

$$= (x^2 + 4)(x^2 - 2x + 2)$$

$$= x^4 - 2x^3 + 2x^2 + 4x^2 - 8x + 8$$

$$\boxed{f(x) = x^4 - 2x^3 + 6x^2 - 8x + 8}$$

8) $3+i, 3-i, -3i, 3i$

$$x = 3+i, x = 3-i, x = -3i, x = 3i$$

$$x-3-i=0 \quad x-3+i=0 \quad x+3i=0 \quad x-3i=0$$

$$f(x) = (x-3-i)(x-3+i)(x+3i)(x-3i)$$

$$= (x^2 - 3x + ix - 3x + 9 - 3i - ix + 3i - i^2)(x^2 + 3ix - 3ix - 9i^2)$$

$$= (x^2 - 6x + 10)(x^2 + 9)$$

$$= x^4 - 6x^3 + 10x^2 + 9x^2 - 54x + 90$$

$$= \boxed{x^4 - 6x^3 + 19x^2 - 54x + 90}$$

State the number of complex zeros and the possible rational zeros for each function. Then find all zeros.

9) $f(x) = x^3 - 3x^2 + x - 3$

degree: 3 \therefore , 3 complex zeros

possible rational zeros: $\frac{\pm 1, \pm 3}{\pm 1} \Rightarrow \pm 1, \pm 3$

$$\begin{array}{r|rrrr} 3 & 1 & -3 & 1 & -3 \\ & \downarrow & 3 & 0 & 3 \\ \hline & 1 & 0 & 1 & 0 \end{array}$$

$$x^2 + 1 = 0$$

$$x^2 = -1$$

$$x = \pm i$$

$$\boxed{\text{zeros: } 3, i, -i}$$

10) $f(x) = x^3 + 5x^2 + x + 5$

degree: 3 \therefore , 3 complex zeros

possible rational zeros: $\frac{\pm 1, \pm 5}{\pm 1} \Rightarrow \pm 1, \pm 5$

$$\begin{array}{r|rrrr} -5 & 1 & 5 & 1 & 5 \\ & \downarrow & -5 & 0 & -5 \\ \hline & 1 & 0 & 1 & 0 \end{array}$$

$$x^2 + 1 = 0$$

$$x^2 = -1$$

$$x = \pm i$$

$$\boxed{\text{zeros: } -5, i, -i}$$

see these steps

$$cPolyRoots(x^3 + 5x^2 + x + 5, x)$$

$$\{-i, i, -5\}$$

$$\boxed{\text{zeros: } -i, i, -5}$$