

## Skill Builder: Topic 3.2 – Implicit Differentiation (Circuit)

Begin in the first cell marked #1 and find the derivative of each given function. To advance in the circuit, search for your answer and mark that cell #2. Continue in this manner until you complete the circuit. Show all pertinent work.

<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># 1</div> <p>Find <math>\frac{dy}{dx}</math> for <math>3\sqrt[3]{x} - 12\sqrt[3]{y^4} = 9</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> <math>-\frac{25}{4}</math> </div>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># ____</div> <p>Find the slope of the tangent line to the graph of <math>2xy^2 + xy = y</math> when <math>y = 1</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> 1                 </div>
<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># ____</div> <p>Find <math>\frac{dy}{dx}</math> for <math>y^2 = \frac{1}{2x+5}</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> <math>-\frac{9}{2}</math> </div>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># ____</div> <p>For the relation <math>\sqrt{x+y} = 3x</math>, find the value of <math>x</math> for which <math>\frac{dy}{dx} = 17</math> when <math>y = 8</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> <math>\frac{1 - y \sec^2(xy)}{x \sec^2(xy) - 1}</math> </div>
<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># ____</div> <p>If <math>\sin y + x = \frac{7}{2}</math>, find the rate of change at the point <math>\left(3, \frac{\pi}{6}\right)</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> <math>\frac{1}{16\sqrt{x^2y}}</math> </div>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># ____</div> <p>Write the y-intercept of the equation of the tangent line to <math>x^2 + y^2 = 25</math> in the third quadrant where <math>x = -3</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> undefined                 </div>
<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># ____</div> <p>Find the slope of the tangent line to the ellipse <math>x^2 + 4y^2 = 16</math> at the point <math>(4, 0)</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> <math>\frac{-1}{y(2x+5)^2}</math> </div>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px;"># ____</div> <p>Find <math>\frac{dy}{dx}</math> for <math>\tan(xy) = x + y</math>.</p>	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin-bottom: 5px; text-align: center;"> <b>Ans:</b> <math>-\frac{2}{\sqrt{3}}</math> </div>