Pre-Calculus 2016-2017

3.3 Logarithmic Functions & Their Graphs

Target 3B: Know and understand the inverse relationships of exponential and logarithmic equations



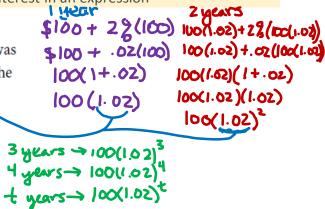
SAT Connection

Passport to Advanced Math

14. Use structure to isolate or identify a quantity of interest in an expression

Example: Jessica opened a bank account that earns 2 percent interest compounded annually. Her initial deposit was \$100, and she uses the expression $$100x^{t}$ to find the value of the account after t years.

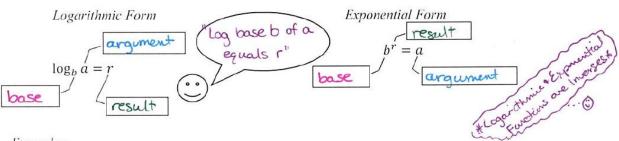
What is the value of x in the expression?



:, x=1.02

Solution

Logarithmic Functions



Examples

Evaluate the logarithmic expression.

$$3 = 9$$

$$3 = 3^2$$

1. log3 9 = C

$$2. \log_3 \frac{1}{27} = C$$

$$3_{\ell} = \frac{3_3}{4}$$

$$3.\log_2\sqrt{8} = \Gamma$$

$$2^{r} = \sqrt{2^{3}}$$

$$2^{c} = (2^{3})^{4}$$

$$2^{5} = 2^{3/2}$$
 $1 = 3/2$

$$-092\sqrt{8} = \frac{3}{2}$$

Common Log \rightarrow has base 10 Logx = Logiox Natural Log → has base _C__ Inx = Logex

Examples

Using a calculator, evaluate the logarithmic expression.

1. log 4

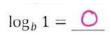
3. $\log_2 5$

.602

693

2.322

Properties of Logs/Natural Logs



$$b^{\circ} = 1$$

$$\log_b b = 1$$

$$b^{|\mathbf{l}|} = b$$

$$e^{it} = e$$

$$\ln e =$$

$$\log_b b^y = \underline{U}$$

$$b^{\frac{1}{2}} = b^{y}$$



$$\ln e^y = y$$

$$b^{\log_b y} = 4$$

$$\log_b = \log_b y$$



$$e^{\ln y} = y$$

Using the properties of logarithms, evaluate the logarithmic expression.

$$1.\log_3 9$$

3.
$$e^{\ln 4}$$







6.
$$\log_{10} \frac{1}{100}$$

7.
$$\ln e^{8}$$

8.
$$x^{\log_x 7}$$





Solve the equation for x.

9.
$$\log x = 5$$

10.
$$2 \log x = -6$$

$$\chi = \frac{1}{103}$$

11.
$$\ln x^2 = 4$$

More Practice

Logarthims

https://www.khanacademy.org/math/algebra2/exponential-and-logarithmic-functions/introduction-to-

logarithms/a/intro-to-logarithms

http://www.themathpage.com/aprecalc/logarithmic-exponential-functions.htm

http://www.sosmath.com/algebra/logs/log4/log41.html

http://www.regentsprep.org/regents/math/algtrig/ATE9/logs.htm

https://youtu.be/Z5myJ8dg_rM

Homework Assignment

p.308 #1-35 odd,59,61

SAT Connection

Solution

The correct answer is 1.02. The initial deposit earns 2 percent interest compounded annually. Thus at the end of 1 year, the new value of the account is the initial deposit of \$100 plus 2 percent of the initial deposit: $$100 + \frac{2}{100} (\$100) = \$100(1.02)$. Since the interest is compounded annually, the value at the end of each succeeding year is the sum of the previous year's value plus 2 percent of the previous year's value. This is again equivalent to multiplying the previous year's value by 1.02. Thus, after 2 years, the value will be $\$100(1.02)(1.02) = \$100(1.02)^2$; after 3 years, the value will be $\$100(1.02)^3$; and after t years, the value will be $\$100(1.02)^t$. Therefore, in the formula for the value for Jessica's account after t years, $\$100(x)^t$, the value of x must be 1.02.