

4.2 MVT

Inc/Dec

f cont on $[a, b]$ + diff'able on (a, b)

$f'(x) > 0$ means f increasing

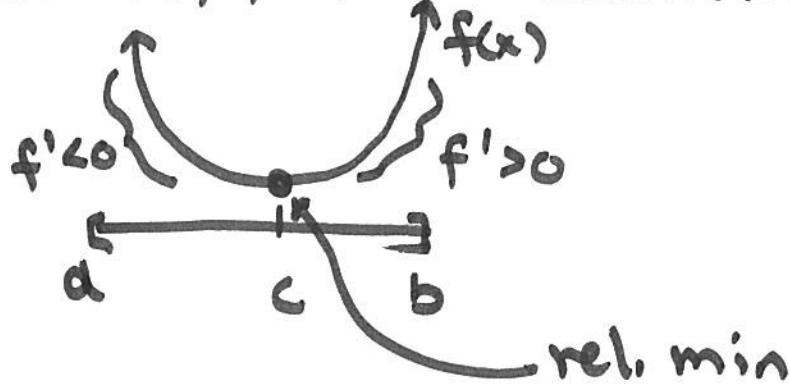
$f'(x) < 0$ means f decreasing

$f'(x) = 0$ means f neither inc nor dec

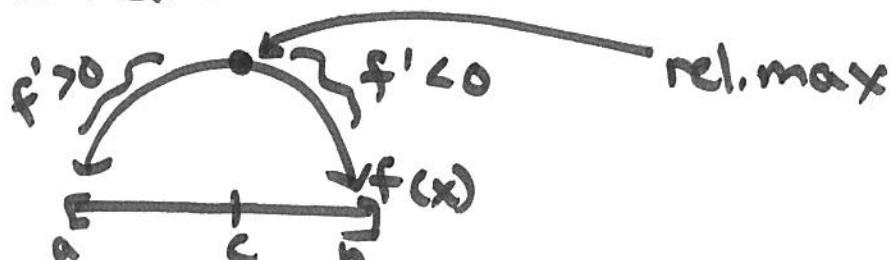
1ST Derivative Test

f cont on $[a, b]$ and c is a critical #,

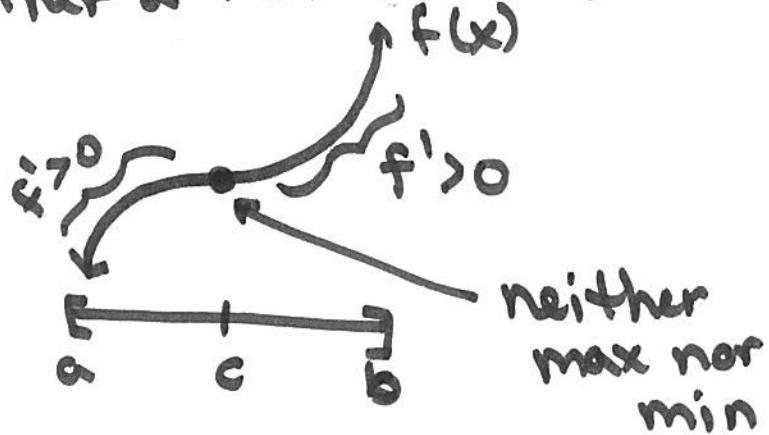
- ① If $f'(x)$ changes from negative to positive, $f(c)$ is a relative min



- ② If $f'(x)$ changes from positive to negative, $f(c)$ is a rel. max



③ If $f'(x)$ doesn't change signs @ $x=c$,
 $f(c)$ is neither a max nor min



where

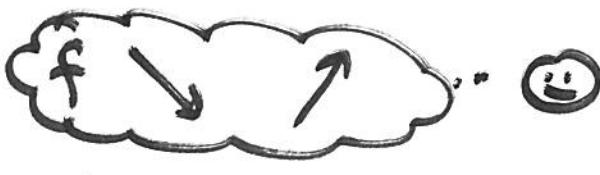
Find $f'(x)$ inc/dec and has rel max/min.

ex: $f(x) = x^2 + 8x + 10$

$\rightarrow f'(x) = 2x + 8$

$2x + 8 = 0 \leftarrow \text{get crit's}$

$x = -4 \leftarrow \text{critical #}$



$$\begin{array}{c} f' \\ \hline - & + \\ \hline -5 & -4 & \textcircled{\text{o}} \end{array}$$

- make f' # line
- put crit # on f' # line
- pick test #s to test into f'

$f' > 0 \rightarrow +$

$f' < 0 \rightarrow -$

$f(x)$ inc on $(-4, \infty)$ b/c $f'(x) > 0$ on that interval

$f(x)$ dec on $(-\infty, -4)$ b/c $f'(x) < 0$ on that interval

$f(x)$ has Rel. min @ $x = -4$ b/c $f'(x)$ changes from neg. to pos. @ $x = -4$

pt $\rightarrow (-4, -6)$
for rel. min

$$f(-4) = (-4)^3 + 8(-4) + 10$$

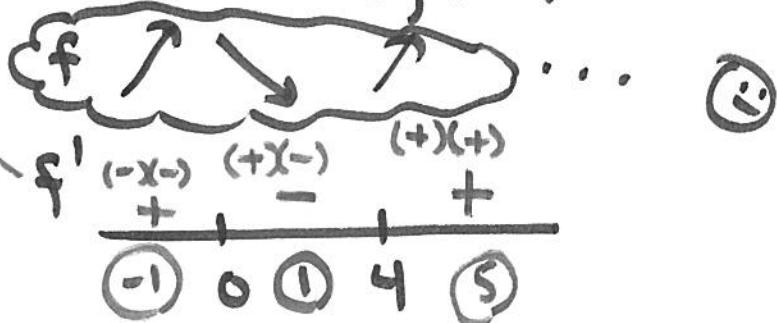
$$\therefore f(x) = x^3 - 6x^2 + 15$$

$$f'(x) = 3x^2 - 12x$$

$$0 = 3x^2 - 12x \leftarrow \text{gt crit's}$$

$$0 = 3x(x-4)$$

$$x=0, x=4 \leftarrow \text{crit's}$$



f inc on $(-\infty, 0) \cup (4, \infty)$ b/c $f' > 0$ on those intervals

f dec on $(0, 4)$ b/c $f' < 0$ on $(0, 4)$

f has rel. min @ $x=4$ b/c f' changes
from neg. to pos
min pt. $(4, -17)$

f has rel. max @ $x=0$ b/c f' changes
from pos. to neg.
max pt. $(0, 15)$