

Let $f$ be a twice-differentiable function defined on the interval $-1.2<x<3.2$ with $f(1)=2$. The graph of $f^{\prime}$, the derivative of $f$, is shown above. The graph of $f^{\prime}$ crosses the $x$-axis at $x=-1$ and $x=3$ and has a horizontal tangent at $x=2$. Let $g$ be the function given by $g(x)=e^{f(x)}$.
(a) Write an equation for the line tangent to the graph of $g$ at $x=1$.
(b) For $-1.2<x<3.2$, find all values of $x$ at which $g$ has a local maximum. Justify your answer.
(c) The second derivative of $g$ is $g^{\prime \prime}(x)=e^{f(x)}\left[\left(f^{\prime}(x)\right)^{2}+f^{\prime \prime}(x)\right]$. Is $g^{\prime \prime}(-1)$ positive, negative or zero? Justify your answer.
(d) Find the average rate of change of $g^{\prime}$, the derivative of $g$, over the interval $[1,3]$.

