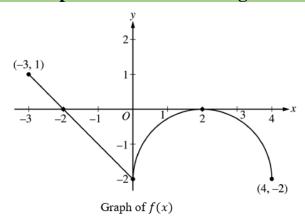
## **Properties of Definite Integrals**



Let f be the function, given by the graph above, defined on the closed interval  $-3 \le x \le 4$  which consists of one line segment and a semicircle. Let  $g(x) = \int_0^x f(t) \, dt$ .

Find g(0), g(4), and g(-3).

## **Properties of Definite Integrals**

$$\int_a^a f(x) \, dx =$$

$$\int_a^b f(x) \, dx =$$

$$\int_a^b f(x) \, dx + \int_b^c f(x) \, dx =$$

$$\int_a^b k \, f(x) \, dx =$$

$$\int_a^b (f(x) \pm g(x)) \, dx =$$

Example:

Given  $\int_{-5}^{5} f(x) dx = 14$ ,  $\int_{5}^{8} f(x) dx = -17$ , and  $\int_{-5}^{5} h(x) dx = 24$ , find:

$$\mathbf{a)} \ \int_5^{-5} f(x) \, dx$$

**b**) 
$$\int_{-5}^{5} (3f(x) - 2h(x)) dx$$

$$\mathbf{c}) \quad \int_{-5}^{8} f(x) \, dx$$