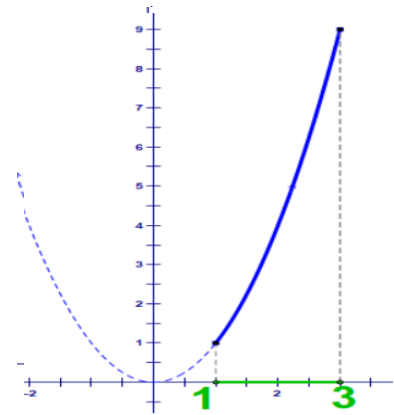


## Lengths of Curves

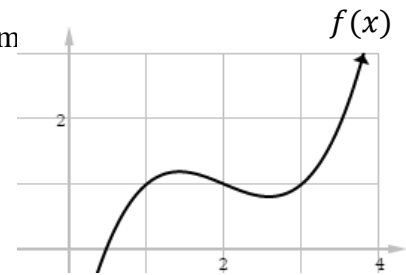
Estimate the length of the curve  $y = x^2$  on  $[1,3]$ .



## Finding the Length of a Curve

Given 2 points  $(x_1, y_1)$  and  $(x_2, y_2)$ , find the distance between them

Distance =

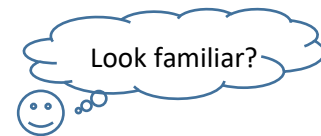


$$\text{Sum of } n \text{ segments} = \sum_{k=1}^n$$

Sum of infinite # of segments

$$= \sum_{k=1}^n$$

$$= \sum_{k=1}^n$$



## Length of a Curve

**Length of a Curve =**  
**(Arc Length)**

*Example 1:*

Find the length of the curve  $y = x^2$  on  $[1,3]$ .

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*Example 2:*

Find the length of the curve  $x = \sin y$  from  $y = 0$  to  $y = \frac{\pi}{2}$ .

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*Example 3:*

Find the length of the curve  $y = \frac{1}{3}(x^2 + 2)^{3/2}$  on  $[0,3]$ .

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*Example 4:*

Find the length of the curve  $y = 2x^{1/5}$  from  $(-32, -4)$  to  $(32,4)$