DATE: _____

Taylor Series

Recall writing a function as a Power Series: $f(x) = c_0 + c_1(x-a) + c_2(x-a)^2 + c_3(x-a)^3 + \dots + c_n(x-a)^n + \dots$ for x = a, f(a) =so, $c_0 =$ $f'(x) = c_1 + 2c_2(x-a) + 3c_3(x-a)^2 + 4c_4(x-a)^3 + \dots + nc_n(x-a)^{n-1} + \dots$ then, f'(a) =so, $c_1 =$ $f''(x) = 2c_2 + 2 \cdot 3c_3(x-a) + 3 \cdot 4c_4(x-a)^2 + \dots + (n-1)n \cdot c_n(x-a)^{n-2} + \dots$ then, f''(a) =so, $c_2 =$ $f'''(x) = 2 \cdot 3c_3 + 2 \cdot 3 \cdot 4c_4(x-a) + \dots + (n-2)(n-1)n \cdot c_n(x-a)^{n-3} + \dots$ then, $f^{\prime\prime\prime}(a) =$ so, $c_3 =$ Do you see a pattern? Predict $f^{(n)}(a) =$ so, $c_n =$ Therefore, a function as a Power Series: $f(x) = c_0 + c_1(x-a) + c_2(x-a)^2 + c_3(x-a)^3 + \dots + c_n(x-a)^n + \dots$ can now be written as the **Taylor Series** $f(x) = + (x-a) + (x-a)^2 + (x-a)^3 + \dots + (x-a)^n + \dots$

 $=\sum_{\infty}^{\infty}$

 $(x-a)^k$

where *f* is generated (centered) @ x = a

Taylor Polynomial of order *n* for f(x) $P_n(x) = + (x-a) + (x-a)^2 + (x-a)^3 + \dots + (x-a)^n$ $= \sum_{k=1}^n (x-a)^k$ where *f* is generated (centered) @ x = a

For a more specific case, we have:

Maclaurin Series $f(x) = + x + x^{2} + x^{3} + \dots + x^{n} + \dots$ $= \sum_{k=1}^{\infty} x^{k}$ where f is generated (centered) @ x = 0

Example 1: Find the Maclaurin Series of $f(x) = e^x$

Example 2: Find the Maclaurin Series of $f(x) = \sin x$