

Rally Coach: Binomial Theorem (Target 7A)

<p>Find the coefficient of the x^2 term in the expansion of $(\frac{2}{a} + \frac{x}{b})^{5+n}$</p> $\binom{5}{2} (2)^3 (x)^2$ $= 10 \cdot 8x^2$ $= 80x^2$ <p style="text-align: right;">80</p>	<p>Find the coefficient of the a^2 term in the expansion of $(2a + 1)^5$</p> $\binom{5}{3} (2a)^2 (1)^3$ $= 10 \cdot 4a^2$ $= 40a^2$ <p style="text-align: right;">40</p>
<p>Find the coefficient of the a^3b^4 term in the expansion of $(a - 3b)^7$</p> $\binom{7}{4} a^3 (-3b)^4$ $= 35a^3 \cdot 81b^4$ $= 2835a^3b^4$ <p style="text-align: right;">2835</p>	<p>Find the coefficient of the x^3y^4 term in the expansion of $(2x - y)^7$</p> $\binom{7}{4} (2x)^3 (-y)^4$ $= 35 \cdot 8x^3 \cdot y^4$ $= 280x^3y^4$ <p style="text-align: right;">280</p>
<p>Find the 2nd term in the expansion of $(y - 2x)^4$</p> <p>$r=2$ $r-1=1$</p> $\binom{4}{1} (y)^3 (-2x)^1$ $= 4 \cdot y^3 \cdot -2x$ $= \boxed{-8xy^3}$	<p>Find the 2nd term in the expansion of $(y - x)^4$</p> <p>$r=2$ $r-1=1$</p> $\binom{4}{1} (y)^3 (-x)^1$ $= 4 \cdot y^3 \cdot -x$ $= \boxed{-4xy^3}$
<p>Find the 10th term in the expansion of $(x + y)^{23}$</p> <p>$r=10$ $r-1=9$</p> $\binom{23}{9} x^{14} y^9$ $= \boxed{817190x^{14}y^9}$	<p>Find the 10th term in the expansion of $(a + b)^{18}$</p> <p>$r=10$ $r-1=9$</p> $\binom{18}{9} a^9 b^9$ $= \boxed{48620a^9b^9}$

Find the 11th term in the expansion of:
 $(2x + y)^{13}$ $r=11, r-1=10$

$$\binom{13}{10} (2x)^3 y^{10}$$

$$= 286 \cdot 8x^3 y^{10}$$

$$= \boxed{2288x^3 y^{10}}$$

Find the 11th term in the expansion of:
 $(x + 2y)^{13}$ $r=11, r-1=10$

$$\binom{13}{10} x^3 (2y)^{10}$$

$$= 286 x^3 \cdot 1024 y^{10}$$

$$= \boxed{292864 x^3 y^{10}}$$

Expand the binomial: $(2x - 3y)^5$

$$\binom{5}{0} (2x)^5 (-3y)^0 + \binom{5}{1} (2x)^4 (-3y)^1 + \binom{5}{2} (2x)^3 (-3y)^2$$

$$+ \binom{5}{3} (2x)^2 (-3y)^3 + \binom{5}{4} (2x)^1 (-3y)^4 + \binom{5}{5} (2x)^0 (-3y)^5$$

$$= \boxed{32x^5 - 240x^4 y + 720x^3 y^2 - 1080x^2 y^3 + 810x y^4 - 243y^5}$$

Expand the binomial: $(3x - 4y)^5$

$$\binom{5}{0} (3x)^5 (-4y)^0 + \binom{5}{1} (3x)^4 (-4y)^1 + \binom{5}{2} (3x)^3 (-4y)^2$$

$$+ \binom{5}{3} (3x)^2 (-4y)^3 + \binom{5}{4} (3x)^1 (-4y)^4 + \binom{5}{5} (3x)^0 (-4y)^5$$

$$= \boxed{243x^5 - 1620x^4 y + 4320x^3 y^2 - 5760x^2 y^3 + 3840x y^4 - 1024y^5}$$

Expand the binomial: $(x^4 - y)^3$

$$\binom{3}{0} (x^4)^3 (-y)^0 + \binom{3}{1} (x^4)^2 (-y)^1 + \binom{3}{2} (x^4)^1 (-y)^2$$

$$+ \binom{3}{3} (x^4)^0 (-y)^3$$

$$= \boxed{x^{12} - 3x^8 y + 3x^4 y^2 - y^3}$$

Expand the binomial: $(x - y^4)^3$

$$\binom{3}{0} (x)^3 (-y^4)^0 + \binom{3}{1} (x)^2 (-y^4)^1 + \binom{3}{2} (x)^1 (-y^4)^2$$

$$+ \binom{3}{3} (x)^0 (-y^4)^3$$

$$= \boxed{x^3 - 3x^2 y^4 + 3x y^8 - y^{12}}$$

Find the 8th term in the expansion of:

$$(a^2 b - cd^3)^{15} \quad r=8, r-1=7$$

$$\binom{15}{7} (a^2 b)^8 (-cd^3)^7$$

$$= \boxed{-6435 a^{16} b^8 c^7 d^{21}}$$

Find the 8th term in the expansion of:

$$(a^3 b - cd^2)^{15} \quad r=8, r-1=7$$

$$\binom{15}{7} (a^3 b)^8 (-cd^2)^7$$

$$= \boxed{-6435 a^{24} b^8 c^7 d^{14}}$$

Expand the binomial: $(\sqrt{x} + \sqrt{3})^3$

$$\binom{3}{0} (\sqrt{x})^3 (\sqrt{3})^0 + \binom{3}{1} (\sqrt{x})^2 (\sqrt{3})^1 + \binom{3}{2} (\sqrt{x})^1 (\sqrt{3})^2$$

$$+ \binom{3}{3} (\sqrt{x})^0 (\sqrt{3})^3$$

$$= \sqrt{x^3} + 3\sqrt{3}x + 9\sqrt{x} + \sqrt{27}$$

$$= \boxed{x\sqrt{x} + 3\sqrt{3}x + 9\sqrt{x} + 3\sqrt{3}}$$

Expand the binomial: $(\sqrt{x} + \sqrt{2})^3$

$$\binom{3}{0} (\sqrt{x})^3 (\sqrt{2})^0 + \binom{3}{1} (\sqrt{x})^2 (\sqrt{2})^1 + \binom{3}{2} (\sqrt{x})^1 (\sqrt{2})^2$$

$$+ \binom{3}{3} (\sqrt{x})^0 (\sqrt{2})^3$$

$$= \sqrt{x^3} + 3\sqrt{2}x + 6\sqrt{x} + \sqrt{8}$$

$$= \boxed{x\sqrt{x} + 3\sqrt{2}x + 6\sqrt{x} + 2\sqrt{2}}$$