

Calculus BC Schedule-- Chapter 9 Infinite Series

<u>Date</u>	<u>Lesson</u>	<u>HW Assignment</u>
25-Feb	9.1 Power Series	HW2 --p.481 #9,13,14,21,54,55, Video on Power Series Theorems
26-Feb	9.1 Power Series	HW3 --p.481 #23,29,33,69,70,71, p. 502 Quick Quiz #1,4
1-Mar	NO SCHOOL --Pulaski Day	NO Additional Homework
2-Mar	9.4 Radius of Convergence	HW4 --p.511 #7,9,11,23,25,27,49
3-Mar	9.4 Radius of Convergence	HW5 --p.511 #15,17,29,31,34,37,41,58
4-Mar	9.5 Testing Convergence at Endpoints	HW6 --p.523 #1,2,5,6,9,11,13,17
5-Mar	9.5 Testing Convergence at Endpoints	HW7 --p.523 #23,24,25,27,30,31
8-Mar	<i>Check & Connect Day</i>	AP Review Practice Problems
9-Mar	9.5 Testing Convergence at Endpoints	HW8 --p.523 #38,39,41,43,47, Video on Power Series
10-Mar	9.2 Taylor Series	HW9 --p.492 #2,3,13,15,19,22,25
11-Mar	9.2 Taylor Series	HW10 --p.492 #5,7,8,24,28,41
12-Mar	9.2 Taylor Series Quick M/C Quiz for Unit 9 (9.1,9.4,9.5)	HW11 --AP Taylor Series Practice
15-Mar	<i>PLT Planning Day</i>	AP Review Practice Problems
16-Mar	9.3 Taylor's Theorem	HW12 --p.500 #1,3,7,27,39,43
17-Mar	9.3 Taylor's Theorem	HW13 --p.500 #13,19,20,23,32,41
18-Mar	9.3 Taylor's Theorem	HW14 --AP Practice Problems
19-Mar	9.5 Testing Convergence at Endpoints	HW15 --AP Series Problems
22-Mar	<i>Check & Connect Day</i>	AP Review Practice Problems
23-Mar	Quick M/C Quiz for Unit 9 Chapter 9 Review	HW16 --p.526 #1,3,7,12,19,21,23,27,37,43,45,47,49,53
24-Mar	Chapter 9 Review	Study for Test
25-Mar	Chapter 9 Test	AP Review Begins! AP Calculus Exam Monday, May 24 @ 8am.

Calculus BC Schedule-- Chapter 9 Infinite Series

Unit 9: Infinite Series

LIM-7

Applying limits may allow us to determine the finite sum of infinitely many terms.

LEARNING OBJECTIVE

LIM-7.A

Determine whether a series converges or diverges. **BC ONLY**

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LIM-7.B

Approximate the sum of a series. **BC ONLY**

ESSENTIAL KNOWLEDGE

LIM-7.A.1

The n th partial sum is defined as the sum of the first n terms of a series. **BC ONLY**

LIM-7.A.2

An infinite series of numbers converges to a real number S (or has sum S), if and only if the limit of its sequence of partial sums exists and equals S . **BC ONLY**

LIM-7.A.3

A geometric series is a series with a constant ratio between successive terms. **BC ONLY**

LIM-7.A.4

If a is a real number and r is a real number such that $|r| < 1$, then the geometric series

$$\sum_{n=0}^{\infty} ar^n = \frac{a}{1-r} \quad \text{BC ONLY}$$

LIM-7.A.5

The n th term test is a test for divergence of a series. **BC ONLY**

LIM-7.A.6

The integral test is a method to determine whether a series converges or diverges. **BC ONLY**

LIM-7.A.7

In addition to geometric series, common series of numbers include the harmonic series, the alternating harmonic series, and p -series. **BC ONLY**

LIM-7.A.8

The comparison test is a method to determine whether a series converges or diverges. **BC ONLY**

LIM-7.A.9

The limit comparison test is a method to determine whether a series converges or diverges. **BC ONLY**

LIM-7.A.10

The alternating series test is a method to determine whether an alternating series converges. **BC ONLY**

LIM-7.A.11

The ratio test is a method to determine whether a series of numbers converges or diverges. **BC ONLY**

EXCLUSION STATEMENT

The n th term test for divergence, and the integral test, comparison test, limit comparison test, alternating series test, and ratio test for convergence are assessed on the AP Calculus BC Exam. Other methods are not assessed on the exam. However, teachers may include additional methods in the course, if time permits.

LIM-7.A.12

A series may be absolutely convergent, conditionally convergent, or divergent. **BC ONLY**

LIM-7.A.13

If a series converges absolutely, then it converges. **BC ONLY**

LIM-7.A.14

If a series converges absolutely, then any series obtained from it by regrouping or rearranging the terms has the same value. **BC ONLY**

LIM-7.B.1

If an alternating series converges by the alternating series test, then the alternating series error bound can be used to bound how far a partial sum is from the value of the infinite series. **BC ONLY**

LIM-8

Power series allow us to represent associated functions on an appropriate interval.

LEARNING OBJECTIVE

LIM-8.A

Represent a function at a point as a Taylor polynomial. **BC ONLY**

LIM-8.B

Approximate function values using a Taylor polynomial. **BC ONLY**

LIM-8.C

Determine the error bound associated with a Taylor polynomial approximation. **BC ONLY**

LIM-8.D

Determine the radius of convergence and interval of convergence for a power series. **BC ONLY**

LIM-8.E

Represent a function as a Taylor series or a Maclaurin series. **BC ONLY**

LIM-8.F

Interpret Taylor series and Maclaurin series. **BC ONLY**

LIM-8.G

Represent a given function as a power series. **BC ONLY**

ESSENTIAL KNOWLEDGE

LIM-8.A.1

The coefficient of the n th degree term in a Taylor polynomial for a function f centered at $x = a$ is $\frac{f^{(n)}(a)}{n!}$. **BC ONLY**

LIM-8.A.2

In many cases, as the degree of a Taylor polynomial increases, the n th degree polynomial will approach the original function over some interval. **BC ONLY**

LIM-8.B.1

Taylor polynomials for a function f centered at $x = a$ can be used to approximate function values of f near $x = a$. **BC ONLY**

LIM-8.C.1

The Lagrange error bound can be used to determine a maximum interval for the error of a Taylor polynomial approximation to a function. **BC ONLY**

LIM-8.C.2

In some situations, the alternating series error bound can be used to bound the error of a Taylor polynomial approximation to the value of a function. **BC ONLY**

LIM-8.D.1

A power series is a series of the form $\sum_{n=0}^{\infty} a_n(x-r)$, where n is a non-negative integer, $\{a_n\}$ is a sequence of real numbers, and r is a real number. **BC ONLY**

LIM-8.D.2

If a power series converges, it either converges at a single point or has an interval of convergence. **BC ONLY**

LIM-8.D.3

The ratio test can be used to determine the radius of convergence of a power series. **BC ONLY**

LIM-8.D.4

The radius of convergence of a power series can be used to identify an open interval on which the series converges, but it is necessary to test both endpoints of the interval to determine the interval of convergence. **BC ONLY**

LIM-8.D.5

If a power series has a positive radius of convergence, then the power series is the Taylor series of the function to which it converges over the open interval. **BC ONLY**

LIM-8.D.6

The radius of convergence of a power series obtained by term-by-term differentiation or term-by-term integration is the same as the radius of convergence of the original power series. **BC ONLY**

LIM-8.E.1

A Taylor polynomial for $f(x)$ is a partial sum of the Taylor series for $f(x)$. **BC ONLY**

LIM-8.F.1

The Maclaurin series for $\frac{1}{1-x}$ is a geometric series. **BC ONLY**

LIM-8.F.2

The Maclaurin series for $\sin x$, $\cos x$, and e^x provides the foundation for constructing the Maclaurin series for other functions. **BC ONLY**

LIM-8.G.1

Using a known series, a power series for a given function can be derived using operations such as term-by-term differentiation or term-by-term integration, and by various methods (e.g., algebraic processes, substitutions, or using properties of geometric series). **BC ONLY**