1. Let f be a function such that $\int f(x)e^x dx = f(x)e^x - \int 4x^3e^x dx$. Find f(x).

2. If
$$f(0) = 6$$
, $f(1) = 3$, $g(0) = 1$, $g(1) = -1$, and $\int_0^1 f'(x)g(x)dx = 4$, find $\int_0^1 f(x)g'(x) dx$

- 3. Let f be the function defined for x > 0, with f(e) = 2 and f', the first derivative of f, given by $f'(x) = x^2 \ln x$. Find f(x).
- **4.** Concert tickets went on sale at noon (t = 0) and were sold out within 9 hours. The number of people waiting in line to purchase tickets at time t is modeled by a twice-differentiable function, $L(t) = -0.4x^4 + 6.4x^3 36.4x^2 + 74.8x + 118$, for $0 \le t \le 9$. Find the average number of people waiting in line during the first 5 hours that tickets were on sale.

5. Evaluate:
$$\frac{d}{dx} \left(\int_0^{x^2} \cos(t^3) \right) dt$$

6. If
$$f'(x) = \frac{10x}{x^2 + x - 6}$$
, find $f(x)$.