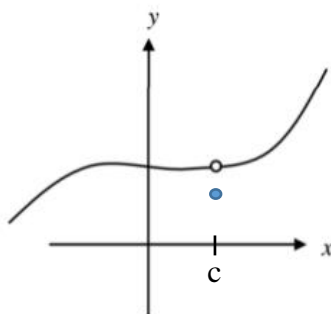


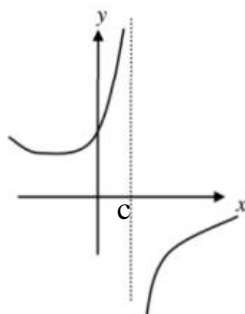
## CONTINUITY

*The idea of continuity:* A function is continuous if you can draw the entire function without lifting your pencil from the paper.

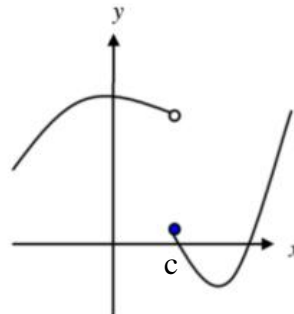
### Types of Discontinuities



Removable Discontinuity  
Hole in the graph



Non-Removable Discontinuity  
Vertical Asymptote



Non-Removable Discontinuity  
Jump

### Definition of Continuity

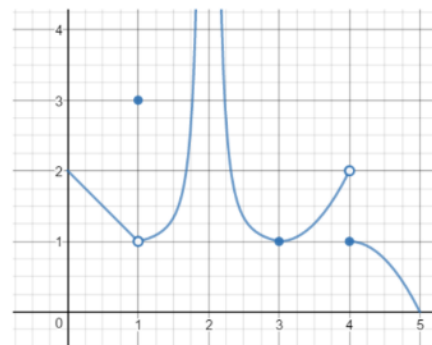
A function is continuous at a point  $x = c$  if  $\lim_{x \rightarrow c} f(x) = f(c)$ .

To prove a function is continuous at  $x = c$ , show:

- ①  $f(c)$  exists
- ②  $\lim_{x \rightarrow c} f(x)$  exists
- ③  $f(c) = \lim_{x \rightarrow c} f(x)$

*Example 1:* Given the graph of the function  $f$  to the right,

a) identify where  $f$  is discontinuous and explain why.



b) identify the interval(s) on which  $f$  is continuous.

*Example 2:* For what values of  $x$  is  $f(x)$  continuous?

$$f(x) = \begin{cases} x^2 - 3x, & x \leq 2 \\ 3, & 2 < x < 4 \\ -1, & x = 4 \\ 7 - x, & x > 4 \end{cases}$$

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*Example 3:* Is  $g(x)$  continuous for all values of  $x$ ?

$$g(x) = \frac{x+3}{x-2}$$

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*Example 4:* Is  $h(x)$  continuous for all values of  $x$ ?

$$h(x) = \frac{x^2-1}{x+1}$$