$\qquad$

1) On the interval $[0,4], h(0)>10$ and $h(4)<10$, but there is no value of $x$ on $[0,4]$ where $h(x)=10$. Explain why this result does not contradict the Intermediate Value Theorem.
2) Steven runs back and forth on a straight track. His velocity, measured in meters per minute, is given by the continuous function, $v(t)$, where $t$ is measured in minutes. Selected values for $v(t)$ are given in the table below.

| $t$ <br> (minutes) | 0 | 1 | 4 | 5 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $v(t)$ <br> $($ meter $/ \mathrm{min})$ | 0 | 70 | 30 | -5 | -7 |

Do the data in the table support the conclusion that Steven's velocity is -10 meters per minute at some time $t$ with $4<t<5$ ?

| $x$ | 0 | 4 | 6 | 8 | 13 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 3 | 4.5 | 3 | 2.5 | 4.4 |

3) The table above shows selected values of a continuous function $f$. For $0 \leq x \leq 13$, what is the fewest possible number of times $f(x)=4$ ?
4) Let $f$ be a function of $x$. Which of the following statements, if true, would guarantee that there is a number $c$ in the interval $[-5,4]$ such that $f(c)=12$ ?

A $f$ is increasing on the interval $[-5,4]$, where $f(-5)=0$ and $f(4)=20$.
(B) $f$ is increasing on the interval $[-5,4]$, where $f(-5)=15$ and $f(4)=30$.
(C) $f$ is continuous on the interval $[-5,4]$, where $f(-5)=0$ and $f(4)=20$.
(D) $f$ is continuous on the interval $[-5,4]$, where $f(-5)=15$ and $f(4)=30$.

